

# Correspondence Analysis

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aka: Dual Scaling, Reciprocal Averaging; Qualitative Correlation ...

Independent 'discovery'

Hotelling 1933; Guttman 1941, Benzécri 1973; Lebart 1984;  
Greenacre 1984; Blasius 1994

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$$\delta_{jk} = \chi_{jk}^2 = L(d_{jk})$$

DATA (2-way, 2mode TABLE)

⇒(decomposed into)

[row-co-ordinates] [column co-ordinates]

- comparable WITHIN
  - only comparable BETWEEN by Projection.
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- Analysis is row-conditional

(each row is profile so  $\sum_i x_{i.} = 1.0$  )

(Or can be chosen to be column-conditional)

... or even doubly-conditional.

**HYPOTHETICAL DISTRIBUTION OF SEATS**  
**IN EUROPEAN PARLIAMENT** (Groenen & Gifi 1989)

	<i>CD</i>	<i>SOC</i>	<i>OTHER</i>	<i>Sum</i>
<i>Belgium</i>	8	9	7	24
<i>Germany</i>	39	30	6	75
<i>Italy</i>	25	11	39	75
<i>Luxemburg</i>	3	2	2	6
<i>Netherlands</i>	13	10	2	25
<i>Sum</i>	88	62	55	205

**BECOMES >>> (FOR C.A. ANALYSIS)**

	<i>CD</i>	<i>SOC</i>	<i>OTHER</i>	<i>Sum</i>
<i>Belgium</i>	.33	.38	.29	1.0
<i>Germany</i>	.52	.40	.08	1.0
<i>Italy</i>	.33	.15	.52	1.0
<i>Luxemburg</i>	.50	.33	.17	1.0
<i>Netherlands</i>	.52	.40	.08	1.0
<i>Mean profile</i>	.43	.30	.26	1.0

## PERFECT SOLUTION:

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**o Christian Democrat**

**#**      **#Lux**    +      **#Italy**  
**Germany &**  
**Netherlands**      **# Belgium**      **o Other**

**o Socialist**

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- ▶ you can compare distances between countries (rows)
  - ▶ you can compare distances between parties (columns)
  - ▶ you CANNOT directly compare distances BETWEEN countries and parties (*except by projection*)
  - ▶ centroid (+) is the “average country”
  - ▶ equality of profiles = zero distance (identity: cf Ger. & Neth.)
  - ▶ “inertia” is (goodness) of fit measure (= %VAF)

## HOW TO COMPARE ROWS & COLUMNS

... *Projection of points on a vector (cf Pro-fit, MDPREF)*

- draw vector from column point through origin
- project row points on to vector (reproduces profile)
- angular separation denotes similarity between profiles/cols.